

‘Color to Gray and back’ using normalization of color components with Cosine, Haar and Walsh Wavelet

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Abstract: The paper shows performance comparison of three proposed methods with orthogonal wavelet alias Cosine, Haar & Walsh wavelet using Normalization for ‘Color to Gray and Back’. The color information of the image is embedded into its gray scale version using wavelet and normalization method. Instead of using the original color image for storage and transmission, gray image (Gray scale version with embedded color information) can be used, resulting into better bandwidth or storage utilization. Among three algorithms considered the second algorithm give better performance as compared to first and third algorithm. In our experimental results second algorithm for DCT wavelet using Normalization gives better performance in ‘Color to gray and Back’ w.r.t all other wavelet transforms in method 1, method 2 and method 3. The intent is to achieve compression of 1/3 and to print color images with black and white printers and to be able to recover the color information as and when required.

Keywords- Color Embedding, Color-to-Gray Conversion, Transforms, Wavelets Normalization , Compression.

I. INTRODUCTION

Digital images can be classified roughly to 24 bit color images and 8bit gray images. We have come to tend to treat colorful images by the development of various kinds of devices. However, there is still much demand to treat color images as gray images from the viewpoint of running cost, data quantity, etc. We can convert a color image into a gray image by linear combination of RGB color elements uniquely. Meanwhile, the inverse problem to find an RGB vector from a luminance value is an ill-posed problem. Therefore, it is impossible theoretically to completely restore a color image from a gray image. For this problem, recently, colorization techniques have been proposed [1]-[4]. Those methods can re-store a color image from a gray image by giving color hints. However, the color of the restored image strongly depends on the color hints given by a user as an initial condition subjectively.

In recent years, there is increase in the size of databases because of color images. There is need to reduce the size of data. To reduce the size of color images, information from all individual color components (color planes) is embedded into a single plane by which gray image is obtained [5][6][7][8]. This also reduces the bandwidth required to transmit the image over the network. Gray image, which is obtained from color image, can be printed using a black-and-white printer or transmitted using a conventional fax machine [6]. This gray image then can be used to retrieve its original color image.

In this paper, we propose three different methods of color-to-gray mapping technique using wavelet transforms and normalization [8][9], that is, our method can recover color images from color embedded gray images with having almost original color images. In method 1 the color information in normalized form is hidden in LH and HL area of first component as in figure 3. And in method 2 the color information in normalize form is hidden in HL and HH area of first component as in figure 3 and in method 3 the color information in normalize form is hidden in LH and HH area of first component as in figure 3. Normalization is the process where each pixel value is divided by 256 to minimize the embedding error [9].

The paper is organized as follows. Section 2 describes transforms and wavelet generation. Section 3 presents the proposed system for “Color to Gray and back” using wavelets. Section 4 describes experimental results and finally the concluding remarks are given in section 5.

II. TRANSFORMS AND WAVELET GENERATION

2.1 Discrete Cosine Transform [9][12]

The NxN cosine transform matrix $C=\{c(k,n)\}$, also called the Discrete Cosine Transform(DCT), is defined as

$$c(k,n) = \begin{cases} \frac{1}{\sqrt{N}} & k=0, 0 \leq n \leq N-1 \\ \sqrt{\frac{2}{N}} \cos \frac{\Pi(2n+1)k}{2N} & 1 \leq k \leq N-1, 0 \leq n \leq N-1 \end{cases} \quad \text{-----(1)}$$

The one-dimensional DCT of a sequence $\{u(n), 0 \leq n \leq N-1\}$ is defined as

$$v(k) = \alpha(k) \sum_{n=0}^{N-1} u(n) \cos \left[\frac{\Pi(2n+1)k}{2N} \right] \quad 0 \leq k \leq N-1 \quad \text{-----(2)}$$

Where $\alpha(0) = \frac{1}{\sqrt{N}}, \alpha(k) = \sqrt{\frac{2}{N}}$ for $1 \leq k \leq N-1$

The inverse transformation is given by

$$u(n) = \sum_{k=0}^{N-1} \alpha(k) v(k) \cos \left[\frac{\Pi(2n+1)k}{2N} \right], \quad 0 \leq n \leq N-1 \quad \text{-----(3)}$$

2.2 Haar Transform [9][10]

The Haar wavelet's mother wavelet function $\varphi(t)$ can be described as

$$\varphi(t) = \begin{cases} 1, & 0 \leq t \leq \frac{1}{2} \\ -1, & \frac{1}{2} \leq t \leq 1 \\ 0, & \text{Otherwise} \end{cases} \quad \text{-----(4)}$$

And its scaling function $\varphi(t)$ can be described as,

$$\varphi(t) = \begin{cases} 1, & 0 \leq t \leq 1 \\ 0, & \text{Otherwise} \end{cases} \quad \text{-----(5)}$$

2.3 Walsh Transform [9][11][12]

Walsh transform matrix is defined as a set of N rows, denoted W_j , for $j = 0, 1, \dots, N-1$, which have the following properties[9]

- W_j takes on the values +1 and -1.
- $W_j[0] = 1$ for all j.
- $W_j \times W_k^T = 0$, for $j \neq k$ and $W_j \times W_k^T$, W_j has exactly j zero crossings, for $j = 0, 1, \dots, N-1$.
- Each row W_j is even or odd with respect to its midpoint.
- Transform matrix is defined using a Hadamard matrix of order N. The Walsh transform matrix row is the row of the Hadamard matrix specified by the Walsh code index, which must be an integer in the range $[0 \dots N-1]$. For the Walsh code index equal to an integer j, the respective Hadamard output code has exactly j zero crossings, for $j = 0, 1 \dots N-1$.

2.4 Wavelets [13]

The first step is to select the transform for which the wavelet need to be generated i.e. let's assume "4 x 4 Walsh transform as shown in Figure 1". The procedure of generating 16x16 Walsh wavelet transform from 4x4 Walsh transform is illustrated in Figure 2.

1	1	1	1
1	1	-1	-1
1	-1	-1	1
1	-1	1	-1

Figure 1: 4x4 Walsh Transform Matrix Figure

	1 st column n of W4 Repeated N=4 times	2 nd column n of W4 Repeated N=4 times	3 rd column n of W4 Repeated N=4 times	4 th column n of W4 Repeated N=4 times
1 to 4 rows	1	1	1	1
	1	1	1	1
	1	1	1	1
	1	1	1	1
5 to 8 rows	1	1	-1	-1
	0	0	0	0
	0	0	0	0
	0	0	0	0
9 to 12 rows	1	-1	-1	1
	0	0	0	0
	0	0	0	0
	0	0	0	0
13 to 16 rows	1	-1	1	-1
	0	0	0	0
	0	0	0	0
	0	0	0	0

Figure 2: Generation of 16x16 Walsh wavelet transform from 4x4 Walsh transform
Wavelets for other transforms can also be generated using the same procedure.

III. PROPOSED SYSTEM

In this section, we propose three new wavelet based color-to-gray mapping algorithm and color recovery method.

3.1 Method 1 [6][7][8]

The 'Color to Gray and Back' has two steps as Conversion of Color to Matted Gray Image with color embedding into gray image & Recovery of Color image back.

3.1.1 Color-to-gray Step

1. First color component (R-plane) of size NxN is kept as it is and second (G-plane) & third (B-plane) color component are resized to N/2 x N/2.
2. Second & Third color component are normalized to minimize the embedding error.
3. Wavelet i.e. DCT, Haar or Walsh wavelet to be applied to first color components of image.
4. First component to be divided into four subbands as shown in figure1 corresponding to the low pass [LL], vertical [LH], horizontal [HL], and diagonal [HH] subbands, respectively.
5. LH to be replaced by normalized second color component, HL to be replace by normalized third color component.
6. Inverse Transform to be applied to obtain Gray image of size N x N.

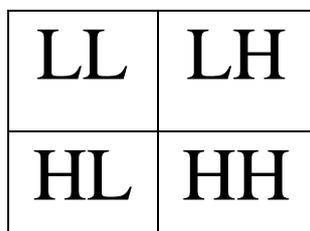


Figure 1: Sub-band in Transform domain

3.1.2 Recovery Step

1. Transform to be applied on Gray image of size N x N to obtain four sub-bands as LL, LH, HL and HH.
2. Retrieve LH as second color component and HL as third color component of size N/2 x N/2 and the the remaining as first color component of size NxN.
3. De-normalize Second & Third color component by multiplying it by 256.

4. Resize Second & Third color component to $N \times N$.
5. Inverse Transform to be applied on first color component.
6. All three color component are merged to obtain Recovered Color Image.

3.2 Method 2 [6][7][8][9]

3.2.1 Color-to-gray Step

1. First color component (R-plane) of size $N \times N$ is kept as it is and second (G-plane) & third (B-plane) color component are resized to $N/2 \times N/2$.
2. Second & Third color component are normalized to minimize the embedding error.
3. Wavelet i.e. DCT, Haar or Walsh wavelet to be applied to first color components of image.
4. First component to be divided into four subbands as shown in figure1 corresponding to the low pass [LL], vertical [LH], horizontal [HL], and diagonal [HH] subbands, respectively.
5. HL to be replaced by normalized second color component, HH to be replaced by normalized third color component.
6. Inverse Transform to be applied to obtain Gray image of size $N \times N$.

3.2.2 Recovery Step

1. Transform to be applied on Gray image of size $N \times N$ to obtain four sub-bands as LL, LH, HL and HH.
2. Retrieve HL as second color component and HH as third color component of size $N/2 \times N/2$ and the remaining as first color component of size $N \times N$.
3. De-normalize Second & Third color component by multiplying it by 256.
4. Resize Second & Third color component to $N \times N$.
5. Inverse Transform to be applied on first color component.
6. All three color component are merged to obtain Recovered Color Image.

3.3 Method 3 [6][7][8][9]

3.3.1 Color-to-gray Step

1. First color component (R-plane) of size $N \times N$ is kept as it is and second (G-plane) & third (B-plane) color component are resized to $N/2 \times N/2$.
2. Second & Third color component are normalized to minimize the embedding error.
3. Wavelet i.e. DCT, Haar or Walsh wavelet to be applied to first color components of image.
4. First component to be divided into four subbands as shown in figure1 corresponding to the low pass [LL], vertical [LH], horizontal [HL], and diagonal [HH] subbands, respectively.
5. LH to be replaced by normalized second color component, HH to be replaced by normalized third color component.
6. Inverse Transform to be applied to obtain Gray image of size $N \times N$.

3.3.2 Recovery Step

1. Transform to be applied on Gray image of size $N \times N$ to obtain four sub-bands as LL, LH, HL and HH.
2. Retrieve LH as second color component and HH as third color component of size $N/2 \times N/2$ and the remaining as first color component of size $N \times N$.
3. De-normalize Second & Third color component by multiplying it by 256.
4. Resize Second & Third color component to $N \times N$.
5. Inverse Transform to be applied on first color component.
6. All three color component are merged to obtain Recovered Color Image.

IV. RESULTS & DISCUSSION

These are the experimental results of the images shown in figure 2 which were carried out on DELL N5110 with below Hardware and Software configuration.

Hardware Configuration:

1. Processor: Intel(R) Core(TM) i3-2310M CPU@ 2.10 GHz.
2. RAM: 4 GB DDR3.
3. System Type: 64 bit Operating System.

Software Configuration:

1. Operating System: Windows 7 Ultimate [64 bit].
2. Software: Matlab 7.0.0.783 (R2012b) [64 bit].

The quality of 'Color to Gray and Back' is measured using Mean Squared Error (MSE) of original color image with that of recovered color image, also the difference between original gray image and reconstructed gray

image (where color information is embedded) gives an important insight through user acceptance of the methodology. This is the experimental result taken on 10 different images of different category as shown in Figure 4. Figure 5 shows the sample original color image, original gray image and its gray equivalent having colors information embedded into it, and recovered color image using method 1, method 2 and method 3 for DCT, Haar and Walsh wavelet transform. As it can be observed that the gray images obtained from these methods does not have any distortion, it does not give any clue that something is hidden in gray image, which is due to the normalizing as it reduces the embedding error.



Figure 4: Test bed of Image used for experimentation.



Original Color
DCT



Original Gray
Walsh



Reconstructed Gray (Method 1)



Reconstructed Gray (Method 1)



Reconstructed Gray (Method 1)



Recovered Color (Method 1)



Recovered Color (Method 1)



Recovered Color (Method 1)



Reconstructed Gray (Method 2)



Reconstructed Gray (Method 2)



Reconstructed Gray (Method 2)



Recoverd Color (Method 2)



Recoverd Color (Method 2)



Recoverd Color (Method 2)



Reconstructed Gray (Method 3)



Reconstructed Gray (Method 3)



Reconstructed Gray (Method 3)



Recoverd Color (Method 3) Recoverd Color (Method 3) Recoverd Color (Method 3)

Figure 5: Color to gray and Back of sample image using Method 1, Method 2 and Method 3

Table 1: MSE between Original Gray-Reconstructed Gray Image

	DCT			Haar			Walsh		
	Method 1	Method 2	Method 3	Method 1	Method 2	Method 3	Method 1	Method 2	Method 3
Img 1	8068.00	8154.70	8106.30	7949.70	8094.80	8025.00	7949.70	8094.80	8025.00
Img 2	16077.00	16099.00	16082.00	16039.00	16081.00	16056.00	16039.00	16081.00	16056.00
Img 3	4961.90	5001.70	4992.00	4892.90	4960.30	4952.80	4892.90	4960.30	4952.80
Img 4	15348.00	15363.00	15363.00	15319.00	15340.00	15354.00	15319.00	15340.00	15354.00
Img 5	5172.40	5176.20	5173.70	5150.50	5169.90	5157.20	5150.50	5169.90	5157.20
Img 6	2264.30	2274.00	2269.20	2246.60	2264.10	2258.50	2246.60	2264.10	2258.50
Img 7	21724.00	21710.00	21764.00	21722.00	21713.00	21760.00	21722.00	21713.00	21760.00
Img 8	26767.00	26783.00	26768.00	26758.00	26781.00	26761.00	26758.00	26781.00	26761.00
Img 9	4735.10	4739.00	4737.30	4727.00	4734.40	4732.20	4727.00	4734.40	4732.20
Img 10	3556.50	3602.80	3560.70	3537.60	3589.10	3548.80	3537.60	3589.10	3548.80
Average	10867.42	10890.34	10881.62	10834.23	10872.76	10860.55	10834.23	10872.76	10860.55

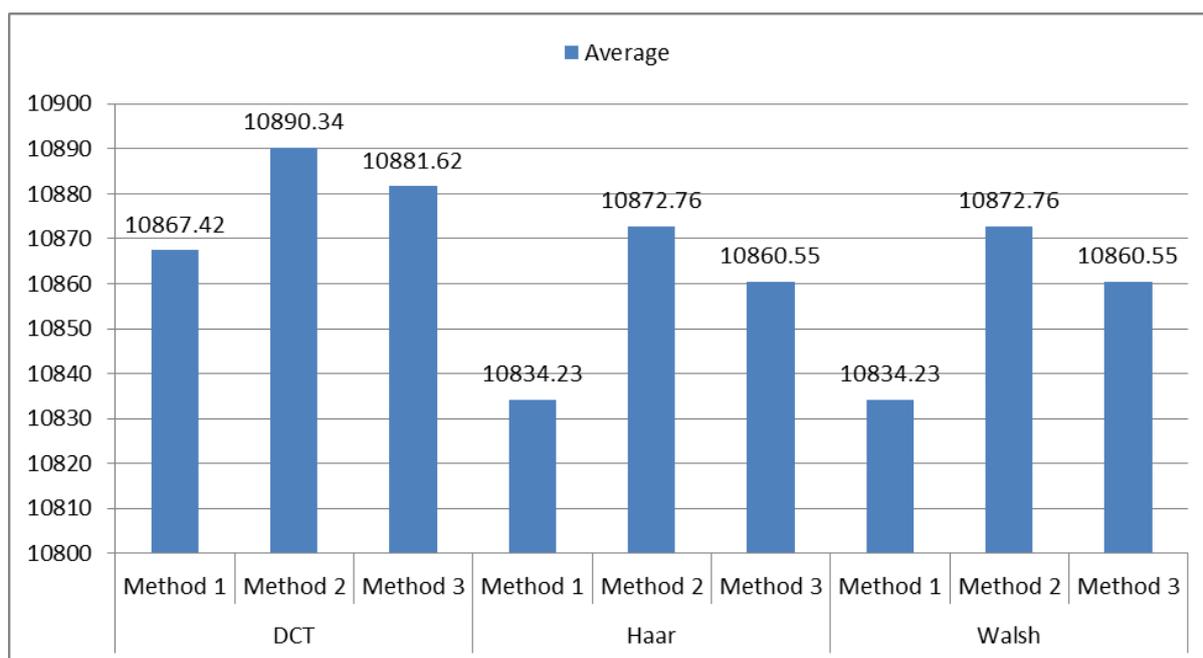


Figure 6: Average MSE of Original Gray w.r.t Reconstructed Gray for Method 1 & Method 2

Table 2: MSE between Original Color-Recovered Color Image

	DCT			Haar			Walsh		
	Method 1	Method 2	Method 3	Method 1	Method 2	Method 3	Method 1	Method 2	Method 3
Img 1	414.1566	349.1929	374.6981	493.5136	386.796	423.3483	493.5136	386.8058	423.3483
Img 2	92.8247	80.1499	83.5076	121.3339	94.1969	99.7293	121.3339	94.1646	99.7293
Img 3	231.7073	195.6875	208.1551	280.6049	219.3106	236.8208	280.6049	219.3244	236.8208
Img 4	93.1414	80.3857	81.8979	116.5854	96.5028	90.456	116.5854	96.5012	90.456
Img 5	25.5738	21.0175	22.9094	41.9297	25.5594	35.3552	41.9297	25.5649	35.3552
Img 6	64.5579	55.7771	57.4603	77.6847	62.8366	64.5713	77.6847	62.844	64.5713
Img 7	271.2525	247.0677	233.6903	278.6486	248.9137	240.0452	278.6486	248.9923	240.0452
Img 8	77.0258	59.6358	73.3799	84.2198	62.8612	78.2887	84.2198	62.8707	78.2887
Img 9	86.3452	75.2929	75.6982	99.8884	83.1166	82.5429	99.8884	83.1185	82.5429
Img 10	396.0637	339.331	361.2053	409.9195	347.9036	368.5165	409.9195	347.9225	368.5165
Average	175.2649	150.3538	157.2602	200.4329	162.7997	171.9674	200.4329	162.8109	171.9674

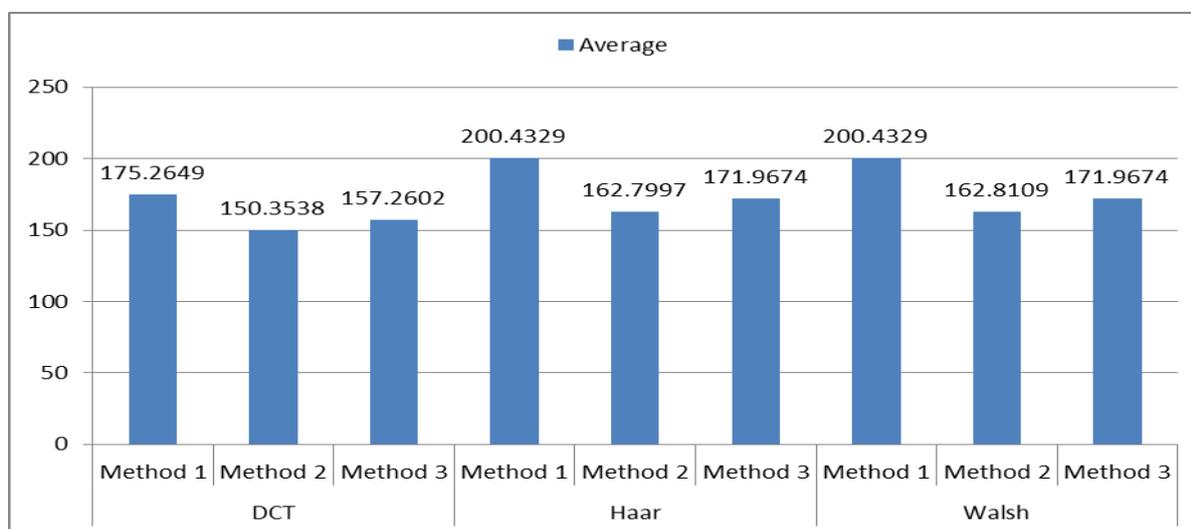


Figure 7: Average MSE of Original Color w.r.t Recovered Color for Method 1 & Method 2

It is observed in Table 2 and Figure 7 that DCT using method 2 gives least MSE between Original Color Image and the Recovered Color Image. Among all considered wavelet transforms, DCT wavelet using method 2 gives best results. And in Table 1 and Figure 6 it is observed that Haar and Walsh wavelet using method 1 gives least MSE between Original Gray Image and the Reconstructed Gray Image. Among all considered wavelet transforms, less distortion in Gray Scale image after information embedding is observed for Haar and Walsh wavelet transform using method 1. The quality of the matted gray is not an issue, just the quality of the recovered color image matters. This can be observed that when DCT wavelet using method 1 is applied the recovered color image is of best quality as compared to other image transforms used in method 1, method 2 and method 3. As in Figure 4 and Table 2 it can be observed that mse between original color image and recovered color is high wherever the granularity of the image is high and it is low wherever the granularity of the image is low.

V. CONCLUSION

This paper have presented three methods to convert color image to gray image with color information embedding into it in two different regions and method of retrieving color information from gray image. These methods allows one to achieve 1/3 compression and send color images through regular black and white fax systems, by embedding the color information in a gray image. These methods are based on transforms i.e DCT, Haar and Walsh wavelet using Normalization technique. DCT wavelet using method 2 is proved to be the best approach with respect to other wavelet transforms using method 1, method 2 and method 3 for 'Color-to-Gray

and Back'. The images with less granularity gives minimum MSE and via. Our next research step could be to test other wavelet transforms and hybrid wavelets for 'Color-to-Gray and Back'.

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BIOGRAPHICAL NOTES



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