Survey on Single image Super Resolution Techniques

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Abstract:*Super-resolution is the process of recovering a high-resolution image from multiple low-resolutionimages of the same scene. The key objective of super-resolution (SR) imaging is to reconstruct a higher-resolution image based on a set of images, acquired from the same scene and denoted as 'low-resolution' images, to overcome the limitation and/or ill-posed conditions of the image acquisition process for facilitating better content visualization and scene recognition. In this paper, we provide a comprehensive review of existing super-resolution techniques and highlight the future research challenges. This includes the formulation of an observation model and coverage of the dominant algorithm – Iterative back projection.We critique these methods and identify areas which promise performance improvements. In this paper, future directions for super-resolution algorithms are discussed. Finally results of available methods are given.*
Keywords: Super-resolution, POCS, IBP, Canny Edge Detection

I.   Introduction

Super resolution is a method for reconstructing a high resolution image from several overlapping low-resolution images[1]. The low resolution input images are the result of re-sampling a high resolution image. The goal is to find the high resolutionimage which, when re-sampled in the lattice of the input images according to the imaging model, predicts well the low resolution input images.

The success of super resolution algorithm is highly dependent on the accuracy of the model of the imaging process.If, for example, the motion computed for some of the images is not correct, the algorithm may degrade the image rather than enhance it.One solution proposed to handle local model inaccuracies and noise is regularization [2].In most cases the enforced smoothness results in the suppression of high-frequency information, and the results are blurred. Regularization may be successful when the scene is strongly restricted, e.g. a binary text image[2].

Applications for super-resolution abound. NASA has been using super-resolution techniques for years to obtain more detailed images of planets and other celestial objects. Closer to home, super-resolution can be used to enhance surveillance videos to more accurately identify objects in the scene. One particular example of this are systems capable of automatically reading license plate numbers from severely pixelated video streams. Another application is the conversion of standard NTSC television recordings to the newer HDTV format which is of a higher resolution.

A variety of approaches for solving the super-resolution problem have been proposed. Initial attempts worked in the frequency domain, typically recovering higher frequency components by taking advantage of the shifting and aliasing properties of the Fourier transform. Deterministic regularization approaches, which work in the spatial domain, enable easier inclusion of *a* priori constraints on the solution space (typically with a smoothness prior). Stochastic methods have received the most attention lately as they generalize the deterministic regularization approaches *and* enable more natural inclusion of prior knowledge. Other approaches include nonuniform interpolation, projection onto convex sets, iterative back projection, and adaptive filtering. With the increased emphasis on stochastic techniques has also come increased emphasis on learning priors from from example data rather than relying on more heuristicallyderived information.

The paper is organized as follows. Section 2 presents Super Resolution Processing and a description of the general model of imaging systems (observation model) that provides the SR image formulations. Section 3 presents the SR image reconstruction approaches that reconstruct a single high-resolution image from a set of given low-resolution images acquired from the same scene. Section 4 presents Results and Discussion. Section 5 discusses several research challenges that remain open in this area for future investigation. Finally, Section.6 concludes this paper.

II.   Super-Resolution Processing

Given a set of low resolution images that result from the observation of the same scene from slightly different views, super resolution algorithm produce a single high resolution image by fusing the input LR images such that the final HR image reproduces the scene with a better fidelity than any of the LR images[11].

The central idea in super resolution processing is to convert the temporal resolution in to spatial resolution. In broad sense, this approach can be used to perform any combination of the following image processing tasks:
- Registration
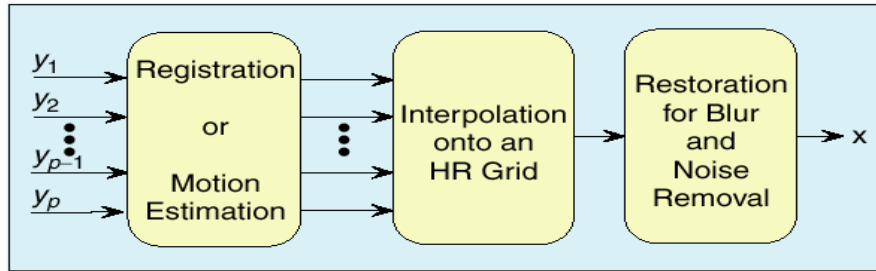- Interpolation
- De-bluriring

Fig.1 Phases of Super-Resolution[3]

First, the SRR algorithm receive several low-resolution corrupted images as the inputs then the registration or Motion Estimation process estimate the relative shifts between LR images compared to the reference LR image with fractional pixel accuracy. Obviously, accurate sub-pixel motion estimation is a very important factor in the success of the SRR algorithm. Since the shifts between LR images are arbitrary, the registered HR image will not always match up to a uniformly spaced HR grid. Thus, non-uniform interpolation is necessary to obtain a uniformly spaced HR image from a composite of non-uniformly spaced LR images. Finally, image restoration(De-blurring) is applied to the up-sampled image to remove blurring and noise.Before presenting the review of existing SR algorithms, we first model the LR image acquisition process.

1.1 Observation Model

Based on the most common observation model (Fig.2) it is considered that the available low-resolution input images are obtained from the high-resolution original scene by warping, blurring and down sampling the scene. Consider the desired HR image of size $L_1 N_1 \times L_2 N_2$ written in lexicographical notation as the vector $x = [x_1, x_2, ..., x_N]^T$ where $N = L_1 N_1 \times L_2 N_2$. Namely,**x** is the ideal un-degraded image that is sampled at orabove the Nyquist rate from a continuous scene which isassumed to be bandlimited. Now, let the parameters *L*1and *L*2 represent the down-sampling factors in the observationmodel for the horizontal and vertical directions, respectively.Thus, each observed LR image is of size $L_1 N_1 \times L_2 N_2$. Let the *k*th LR image be denoted in lexicographicnotation as $y_k = [y_{k,1}, y_{k,2}, ..., y_{k,M}]^T$ for $k = 1, 2, .., p$ and $M = L_1 N_1 \times L_2 N_2$. Now, it is assumed that **x**remains constant during the acquisition of the multipleLR images, except for any motion and degradation allowedby the model. Therefore, the observed LR imagesresult from warping, blurring, and subsampling operatorsperformed on the HR image **x**. Assuming that eachLRimage is corrupted by additive noise, we can then represent the observation model as [3],

$$y_k = DB_k M_k X + n_k \text{ for } 1 \leq k \leq p \tag{1}$$

Where M_k is awarpmatrix of size $L_1 N_1 L_2 N_2 \times L_1 N_1 L_2 N_2$, B_k represents a $L_1 N_1 L_2 N_2 \times L_1 N_1 L_2 N_2$ blur matrix, D is a $(N_1 N_2)^2 \times L_1 N_1 L_2 N_2$ subsampling matrix, and n_k represents a lexicographically ordered noise vector. Ablock diagram for the observation model is illustrated in Fig.2.
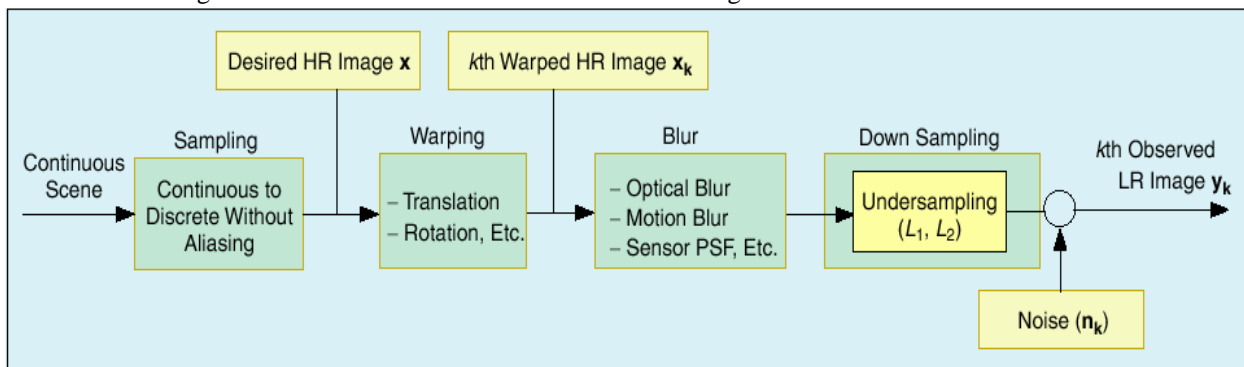

Fig.2 Observation Model

III.   Super-resolution techniques

Image super resolution techniques can be mainly categorized as reconstruction based techniques and learning based techniques.

Table 1 Comparison between Frequency Domain and Spatial Domain Super Resolution Techniques

	Frequency Domain	Spatial Domain
Observation model	**Frequency domain**	**Spatial domain**
Motion Model	**Global Translation**	**Almost Unlimited**
Degradation model	**Global translation**	**Almost unlimited**
Noise model	**Limited**	**Almost unlimited**
A-priori information	**Limited**	**Almost unlimited**
Simplicity	**Very Simple**	**Generally Complex**
Computational Cost	**Low**	**High**
Regularization	**Limited**	**Excellent**
Extensibility	**Poor**	**Excellent**
Applicability	**Limited**	**Wide**
Performance	**Good for Specific Application**	**Good**

In learning based approach, the relationship between an LR image and its corresponding high resolution (HR) image is examined via a pair of LR and HR patches. The training data is used to predict the higher-resolution image[4]. Reconstruction based approach can be employed in the frequency domain or spatial domain. Reconstruction based approach require either single image or multiple low resolution image. Simplicity in theory is a major advantage of the frequency domain approach. In addition, the frequency approach is also convenient for parallel implementation. However, this approach allows low flexibility to add priori constraints, noise models, and spatially varying degradation models. Thus, the development in practical use is limited. On the other hand, spatial domain techniques are more flexible in incorporating priori constraints and have better performance in reconstructed images. Nevertheless, these methods also have drawbacks such as complicated theoretical work and relatively large amount of computation load. A comparison of the two main classes of super-resolution techniques, frequency domain and spatial domain, is found in Table 1[5-9].

1.2 Frequency Domain Approach

The super-resolution problem was posed, along with a frequency domain solution, by Tsai and Huang[10]. Prior to their paper, interpolation was the best technique for increasing the resolution of images. The frequency domain approach makes explicit use of the aliasing that exists in each LR image to reconstruct an HR image. Tsai and Huang [10] first derived a system equation that describes the relationship between LR images and a desired HR image by using the relative motion between LR images. The frequency domain approach is based on the following three principles: i) the shifting property of the Fourier transform, ii) the aliasing relationship between the continuous Fourier transform (CFT) of an original HR image and the discrete Fourier transform (DFT) of observed LR images, iii) and the assumption that an original HR image is band limited. These properties make it possible to formulate the system equation relating the aliased DFT coefficients of the observed LR images to a sample of the CFT of an unknown image. For example, let us assume that there are two 1-D LR signals sampled below the Nyquist sampling rate. From the above three principles, the aliased LR signals can be decomposed into the de-aliased HR signal as shown in Fig. 3.
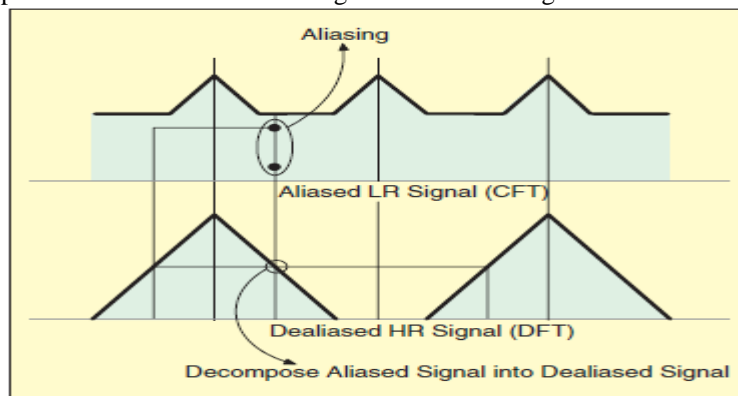
Fig.3. Aliasing relationship between LR image and HR image

Frequency-domain super resolution method typically rely on familiar Fourier transform properties, specifically the shifting and sampling theorems. Since these properties are generally very well known and understood, the frequency domain approaches are easy to grasp and are intuitively appealing. Many of the frequency-domain approaches are based on assumptions which enable the use of efficient procedures for computing the restoration, the most important of which is the Fast Fourier Transform (FFT).

Let $x(t_1, t_2)$ denote a continuous HR image and $X(w_1, w_2)$ be its CFT. The global translations, which are the only motion considered in the frequency domain approach, yield the kth shifted image of $x_k(t_1, t_2) = x(t_1 + \delta_{k1}, t_2 + \delta_{k2})$, where δ_{k1} and δ_{k2} are arbitrary but known values, and $k = 1, 2, .., p$. By the shifting property of the CFT, the CFT of the shifted image, $X_k(w_1, w_2)$, can be written as

$$X_k(w_1, w_2) = \exp[j2\pi(\delta_{k1}w_1 + \delta_{k2}w_2)]X(w_1, w_2) \qquad (2)$$

The shifted image $x_k(t_1, t_2)$ is sampled with the sampling period $T1$ and $T2$ to generate the observed LR image $y_k(n_1, n_2)$. From the aliasing relationship and the assumption of bandlimitedness of $X(w_1, w_2)$ ($|X(w_1, w_2)|) = 0$ for $|w_1| \geq (L_1\pi / T_1)$, $|w_2| \geq (L_2\pi / T_2))$, the relationship between the CFT of the HR image and the DFT of the kth observed LR image can be written as [11]

$$\gamma_k(\Omega_1, \Omega_2) = \frac{1}{T_1 T_2} \sum_{n_1=0}^{L_1-1} \sum_{n_2=0}^{L_2-1} X_k \times \left[\frac{2\pi}{T_1}\left[\frac{\Omega_1}{N_1} + n_1 \right], \frac{2\pi}{T_2}\left[\frac{\Omega_2}{N_2} + n_2 \right] \right] \qquad (3)$$

By using lexicographic ordering for the indices $n1$, $n2$ on the right-hand side and k on the left-hand side, a matrix
vector form is obtained as:
$$Y = \Phi X \qquad (4)$$
where **Y** is a $p \times 1$ column vector with the kth element of the DFT coefficients of $y_k[n_1, n_2]$, **X** is a $L_1 L_2 \times 1$ column vector with the samples of the unknown CFT of $x(t_1, t_2)$, and Φ is a $p \times L_1 L_2$ matrix which relates the DFT of the observed LR images to samples of the continuous HR image. Therefore, the reconstruction of a desired HR image requires us to determine Φ and solve this inverse problem. An extension of this approach for a blurred and noisy image was provided by Kim et al. [12], resulting in a weighted least squares formulation. In their approach, it is assumed that all LR images have the same blur and the same noise characteristics. This method was further refined by Kim and Su [13] to consider different blurs for each LR image. Here, the Tikhonov regularization
method is adopted to overcome the ill-posed problem resulting from blur operator. Bose et al. [14] proposed the recursive total least squares method for SR reconstruction to reduce effects of registration errors (errors in Φ). A discrete cosine transform (DCT)-based method was proposed by Rhee and Kang [15]. They reduce memory requirements and computational costs by using DCT instead of DFT. They also apply multichannel adaptive regularization parameters to overcome ill-posedness such as underdetermined cases or insufficient motion information cases. Theoretical simplicity is a major advantage of the frequency domain approach. That is, the relationship between LR images and the HR image is clearly demonstrated in the frequency domain. The frequency method is also convenient for parallel implementation capable of reducing hardware complexity.

1.3 Spatial Domain Approach
In this class of SR reconstruction methods, the observation model is formulated, and reconstruction is effected in the spatial domain. The linear spatial domain observation model can accommodate global and non-global motion, optical blur, motion blur, spatially varying PSF, non-ideal sampling, compression artifacts and more. Spatial domain reconstruction allows natural inclusion of (possibly nonlinear) spatial domain *a-priori* constraints (e.g. Markov random fields or convex sets) which result in bandwidth extrapolation in reconstruction. Consider estimating a SR image z from multiple LR images $y_r, r \in \{1, 2, ..., R\}$. Images are written as lexicographically ordered vectors. y_r and z are related as $y_r = H_r z$. The matrix H_r, which must be estimated, incorporates motion compensation, degradation effects and subsampling. The observation equation may be generalized to Y = Hz + N where $Y = [y_1^T ... y_R^T]^T$ and $H = [H_1^T ... H_R^T]^T$ with N representing observation noise.

Since the superresolution problem is fundamentally ill-posed, incorporation of prior knowledge is essential to achieve good results. A variety of techniques exist for the super-resolution problem in the spatial domain. These solutions include interpolation, deterministic regularized techniques, stochastic methods, iterative back projection, and projection onto convex sets among others. The primary advantages to working in the spatial domain are support for unconstrained motion between frames and ease of incorporating prior knowledge into the solution.

3.2.1 Interpolation of Non Uniformly Spaced Samples

Registering a set of LR images using motion compensation results in a single, dense composite image of non uniformly spaced samples. A SR image may be reconstructed from this composite using techniques for reconstruction from non-uniformly spaced samples. Unfortunately, this technique generally works very poorly because of some inherent assumptions; the main problem being that camera sensors do not act as impulse functions. Since the observed data result from severely under sampled, spatially averaged areas, the reconstruction step (which typically assumes impulse sampling) is incapable of reconstructing significantly more frequency content than is present in a single LR frame. Degradation models are limited, and no *a-priori* constraints are used. There is also question as to the optimality of separate merging and restoration steps.

3.2.2 Deterministic Regularization

The deterministic regularized SR approach solves the inverse problem by using the prior information about the solution which can be used to make the problem well posed. For example, CLS can be formulated by choosing an **x** to minimize the Lagrangian [16]

$$[\sum_{k=1}^{p} \| y_k - W_k x \|^2 + \alpha \| Cx \|^2] \tag{5}$$

where the operator **C** is generally a high-pass filter, and $\|.\|$ represents a *l2* -norm. In eq(5), a priori knowledge concerning a desirable solution is represented by a smoothness constraint, suggesting that most images are naturally

smooth with limited high-frequency activity, and therefore it is appropriate to minimize the amount of high-pass energy in the restored image. In eq(5), α represents the Lagrange multiplier, commonly referred to as the regularization parameter, that controls the tradeoff between fidelity to the data (as expressed by

$$\sum_{k=1}^{p} \| y_k - W_k x \|^2$$) andsmoothness of the solution (as expressed by $\| Cx \|^2$). TheLarger values of α will

generally lead to a smoothersolution.This is useful when only a small number of LR imagesare available (the problem is underdetermined) orthe fidelity of the observed data is low due to registrationerror and noise. On the other hand, if a large number ofLR images are available and the amount of noise is small,smallαwill lead to a good solution. The cost functional ineq(6) is convex and differentiable with the use of a quadraticregularization

term. Therefore, we can find a unique estimateimage $\hat{x}$ which minimizes the cost functional in eq(5).
One of the most basic deterministic iterative techniquesconsiders solving

$$\left[\sum_{k=1}^{p} W_k^T W_k + \alpha C^T C \right] \hat{X} = \sum_{k=1}^{p} W_k^T y_k \tag{6}$$

and this leads to the following iteration for $\hat{x}$:

$$\hat{X}^{(n+1)} = \hat{X}^{(n)} + \beta \left[\sum_{k=1}^{p} W_k^T \left(y_k - W_k \hat{X}^{(n)} \right) - \alpha C^T C \hat{X}^{(n)} \right] \tag{7}$$

where β represents the convergence parameter and W_k^T contains an up-sampling operator and a type of blur andwarping operator.

3.2.3 Projection Onto Convex Sets(POCS)

Another method for reducing the space of possible reconstructions is projection onto convex sets (POCS). The POCS method describes an alternative iterative approach to incorporating prior knowledge about the solution into the reconstruction process. With the estimates of registration parameters, this algorithm simultaneously solves the restoration and interpolation problem to estimate the SR image. This is a set-theoretic approach where each piece of *a priori* knowledge is formulated as a constraining convex set. Once the group of

convex sets is formed, an iterative algorithm is employedto recover a point on the intersection of the convex sets,

$$g_{i+1} = P_M P_{M-1} ..... P_2 P_1 \{g_i\}$$
(8)

where P_j is the projection of a given point onto the jth convex set and *M* is the number of convex sets. In essence, we are restricting the final restored image to lie on the intersection of the constrainingsets, $\{P_j\}_{j=1}^M$. The reason we require *convex* sets is that convergenceis guaranteed for the case where each set is convex.

One potential group of convex sets is based on the *l2* distance measure,

$$G_k = \{ g \parallel W_k g - y_k \parallel^2 \le 1 \}, 1 \le k \le K$$
(9)

This defines a set of ellipsoids (one for each input image) and restrictsthe final solution to lie inside the ellipsoids. Other possibleconvex sets include ones based on the *l¥* norm, those imposingsmoothness, and those constraining the image intensity to be positive.Two problems with the POCS approach are that uniqueness isnot guaranteed for the final recovered image and that defining theprojections P_j can be difficult.

3.2.4 Iterative Back Projection(IBP)

Super resolution of the image is model as an inverse problem. That is the goal of super resolution is to reverse the effect of the down sampling, blurring and warping that relate the LR image to desired HR image. Mathematically it
is written as

$$y = (X * W) \downarrow S$$
(10)

Where, *X* is original HR image; *y* is LR image; *W* is degeneration function; $\downarrow s$ is down sampling process.

In IBP approach HR image is estimated by back projecting the difference between the simulated LR image and captured LR on interpolated image. This iterative process of SR does iterations until the minimization of the cost function is achieved. Block diagram of IBP algorithm is given in Fig. 4. Mathematically the SR step according to IBP is written as

$$X = X^{(0)} + X_e$$
(11)

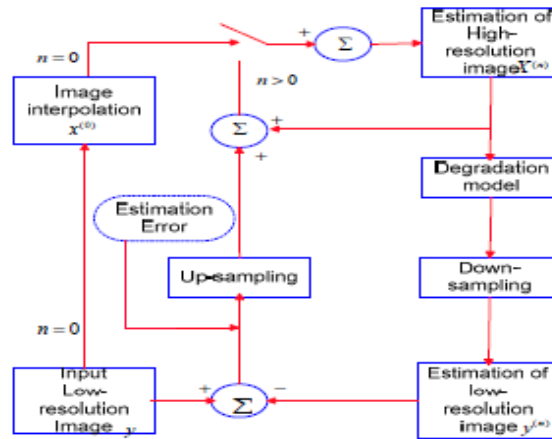Where, X is interpolated image; X_e is error correction.

Fig. 4 Simple IBP Algorithm[17]

Given only one LR input image, the updating procedure can be summarized as doing the following two steps iteratively:

1) Compute the LR error as

$$X_e^{(n)} = (y - y^{(n)}) \uparrow S$$
(12)

Estimation of the simulated LR image is given as

$$y^{(n)} = (X^{(n)} * W) \downarrow S$$
(13)

2) Update the HR image by back-projecting the error as equation (11).

3.2.4.1 Proposed IBP using Canny Edge Detection

Though IBP method can minimize the restoration error significantly in iterative manner and gives good effect, it projected the error back without edge guidance. In proposed algorithm, extra high frequency information is added by Canny edge detection and difference error of up-sampled images from initial and simulated LR images and so that it works as edge preserving algorithm. Block diagram of proposed algorithm is shown in Fig. 5. Steps for proposedalgorithm are given in Table II.
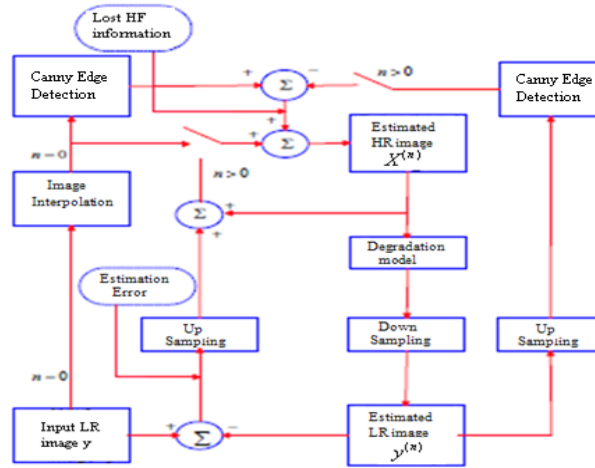

Fig. 5 Canny Edge Detection Algorithm

Mathematically SR according to proposed algorithm is written as

$$X = X^{(0)} + X_e + X_H \tag{14}$$

Where, $X^{(0)}$ is initial interpolated image; X_e is error correction; X_H is high frequency estimation given by

$$X_H = (X * H_{Canny}) \tag{15}$$

Where X_H is the estimated HR image, H_{Canny} is the Canny Edge High Pass filter.

In Summary, proposed algorithm in mathematical form is expressed as below. The estimated HR image after n iterations is given by

$$X^{(n+1)} = X^{(n)} + X_e + X_H^{(n)} \tag{16}$$

The estimation of the high frequency is given as

$$X_H^{(n)} = X_H^{(0)} - \{((y^{(n)}) \uparrow S) * H_{Canny}\} \tag{17}$$

Where $X_H^{(0)}$ is high frequency component of image $X^{(0)}$. The formula for $X_H^{(0)}$ is given as

$$X_H^{(0)} = (X^{(0)} * H_{Canny}) \tag{18}$$

So, the final iterations process given in (13) is rewritten for the combination of IBP and Canny Edge as

$$X^{(n+1)} = X^{(n)} + (y - y^{(n)}) \uparrow S + \{X_H^{(0)} - \{((y^{(n)} \uparrow S) * H_{Canny}\}\} \tag{19}$$

Table II Steps of Canny Edge Detection Algorithm

NO	STEPS
1	Read ground truth image
2	Apply Gaussian blurring and down sampling to generate observed LR image
3	Apply initial interpolation on observed LR image for initial estimation of HR image
4	Apply Canny Edge on initial estimated HR image to obtain high frequency component
5	Apply degradation on initial estimated HR image to generate simulated LR image
6	Apply Canny Edge on simulated LR image
7	Subtract simulated LR from Observed LR image that gives error correction
8	Subtract step 6 output from step 4 output to get lost high frequency component
9	Take summation of step 3 output with step 8 output. This will give improvement in quality of initial estimated HR image
10	Now, this improved HR becomes our initial estimated HR image for the second iteration
11	Repeat step 5 to step 10 until some predefined iteration

IV.   Result and Discussion

To evaluate the SR systems effectively, this work assumes that the original HR images exist and the image qualitydegradation is resulted from Gaussian blurring, and such Gaussian blurring function is known.
To present the performance of this algorithms, several images are tested and results are compared with Nearest Neighbourhood interpolation(NN), Bilinear interpolation (BI), bicubic interpolation (BC), POCS, IBP and IBP + Canny Edge Detection.The image quality is determined based on PSNR evaluation.

As performance criteria, Peak Signal to Noise Ratio (PSNR) is calculated. The mathematical equations for $M \times N$ image analysis are as given bellow[18].
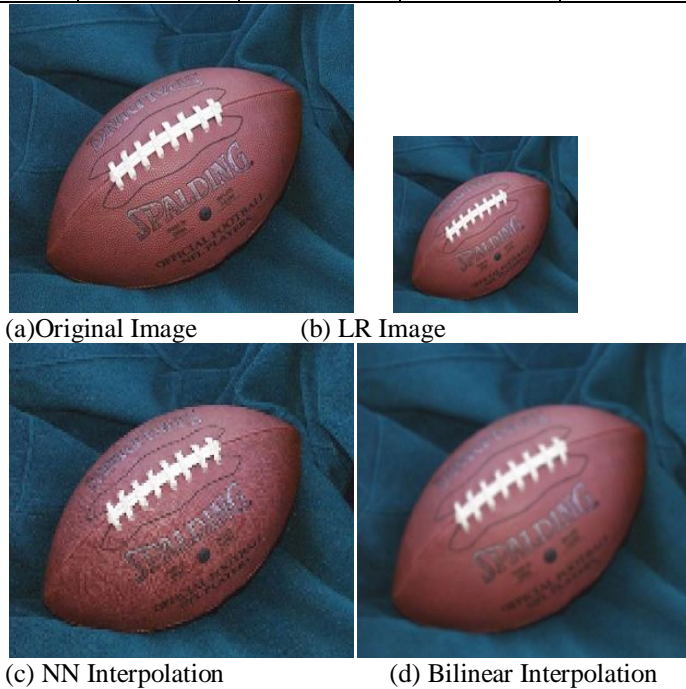
$$MSE = \frac{\sum_i \sum_j [X(i,j) - X^{(n)}(i,j)]^2}{M \times N}$$
(20)

$$PSNR = 10 \log_{10}\left(\frac{255 \times 255}{MSE}\right)$$
(21)

Where, $X(i,j)$ is the original HR image and $X^{(n)}(i,j)$ is the estimated HR image through this algorithm.

The image quality is determined based on PSNR evaluation. A good reconstruction algorithm generally provides low value of MSE and high value of MSSIM and PSNR. The resultant images are shown in figure 6 and 7 . PSNR is obtained using various techniques are given in Table III.

Table III PSNR Comparison

Test Image	Single Frame Algorithms					
	NN	BI	Bicubic	POCS	IBP	IBP +Canny Edge
Apple	26.6500	29.1617	31.6337	30.7417	28.7719	42.3146
Football	26.9158	29.3864	30.4000	30.3136	29.2219	42.8838
Greens	19.9802	22.1634	24.6540	28.2204	22.1575	34.4326
Monkey	29.6891	31.2404	33.4968	32.7840	31.0809	43.6170
Flower	29.1997	32.0320	33.9559	32.4331	31.7295	46.0387
Fruits	28.4520	31.0726	34.1511	32.9744	30.9810	43.7963

(a)Original Image   (b) LR Image

(c) NN Interpolation   (d) Bilinear Interpolation

(e) Bicubic Interpolation   (f) POCS

(g) IBP   (h) IBP + Canny Edge
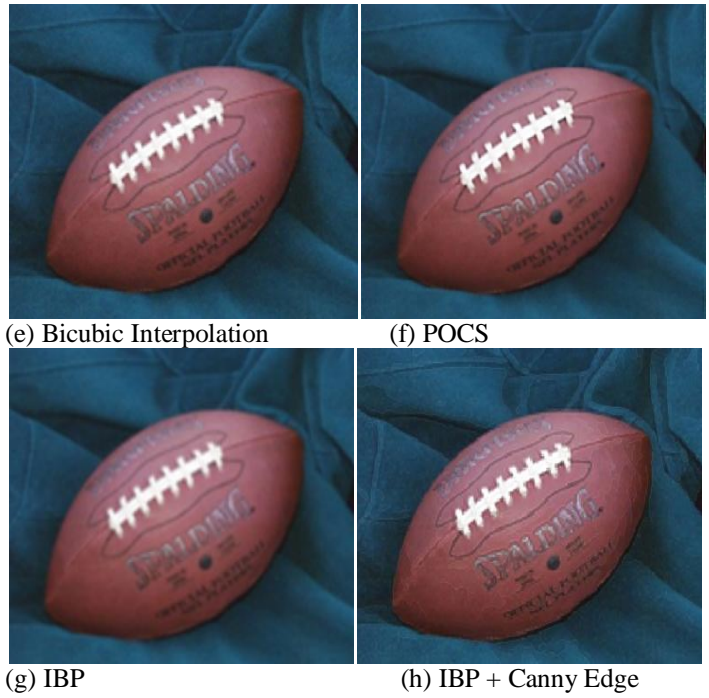
Fig.6. Resultant football Image using different Algorithms

(a)Original Image   (b) LR Image

(c) NN Interpolation   (d) Bilinear Interpolation

(e) Bicubic Interpolation   (f) POCS

(g) IBP   (h) IBP + Canny Edge
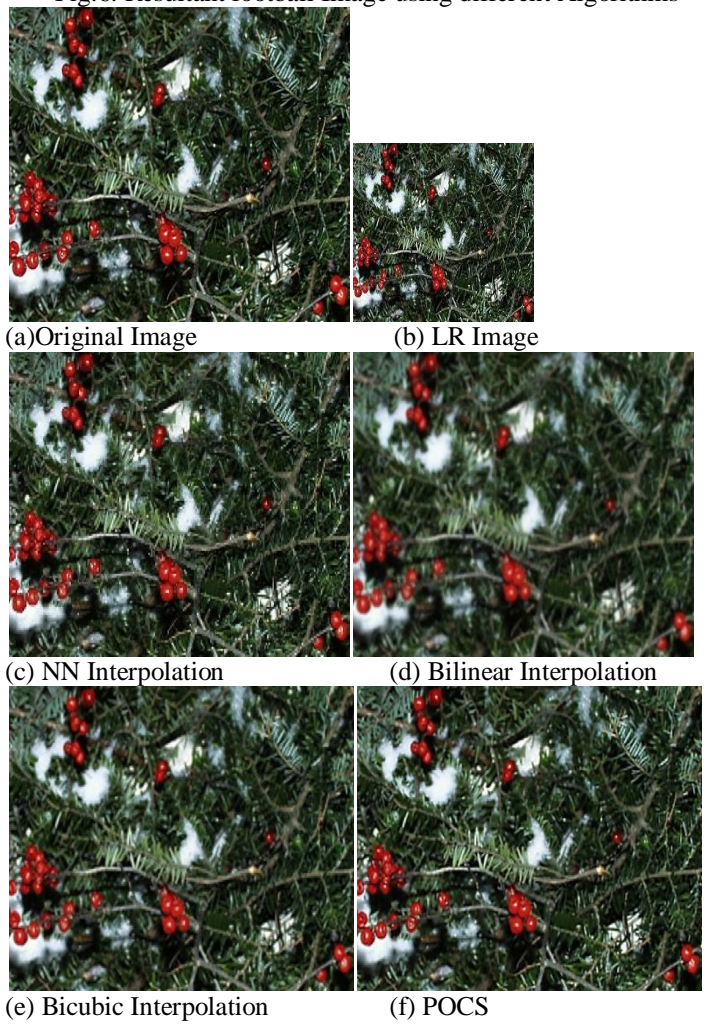Fig.7. Resultant Greens Image using different Algorithms

V.   Future Research Directions

we have identified some new directions for future research. The first asks the question "Can we design camera sensors that are optimal for super-resolution algorithms?".Current CCDs act like box functions, spatially integrating over a uniform rectangular region for each pixel. It is likely that other types of sampling, such as integration over a Gaussian function, would yield better results.

Another direction is to combine super-resolution with dense stereo reconstruction. Dense stereo reconstruction is the process of estimating the depth of every point in the scene from two or more input images taken from different poses. Current techniques typically estimate depths for every pixel in one of the images, but it should be possible to obtain depths on a finer grid by combining super-resolution techniques with dense stereo.

A third potential problem is to combine high dynamic range imaging with super-resolution. High dynamic range imaging involves taking multiple images from the same viewpoint at different *exposures* and then combining the images to obtain an image of higher dynamic range. By taking multiple images at different exposures and with slight translational offsets it might be possible to obtain a super-resolved high dynamic range image more efficiently than if the two stages are done independently.

VI.   Conclusion

The SR imaging has been one of the fundamental image processing research areas. It can overcome or compensate the inherent hardware limitations of the imaging system to provide amore clear image with a richer and informative content. We have provided a review of the current state of super-resolution research, covering the past, present, and future of the problem. A standard image formation model was first introduced, followed by summaries of the major classes of algorithms including frequency domain approaches, deterministic regularization, projection onto convex sets, Iterative Back Projection and Proposed IBP with Canny Edge Detection. In this survey paper, our goal is to offer new perspectives and outlooks of SR imaging research, besides giving an updated overview of existing SR algorithms. It is our hope that this work could inspire more image processing researchers endeavoring on this fascinating topic and developing more novel SR techniques along the way. Finally we discussed potential future directions for research.

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