

New Method of Computing π value (Siva Method)

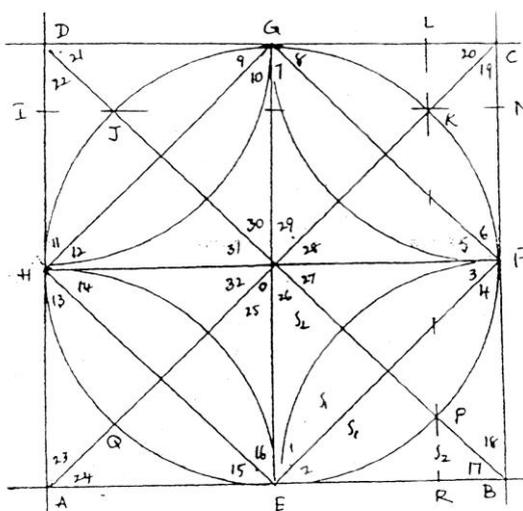
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I. Introduction

π equal to 3.1415926... is an approximation. It has ruled the world for 2240 years. There is a necessity to find out the **exact** value in the place of this approximate value. The following method gives the **total** area of the square, and also the **total** area of the inscribed circle. π derived from this area is thus exact.

II. Construction procedure

Draw a circle with center 'O' and radius $a/2$. Diameter is 'a'. Draw 4 equidistant tangents on the circle. They intersect at A, B, C and D resulting in ABCD square. The side of the square is also equal to diameter 'a'. Draw two diagonals. E, F, G and H are the mid points of four sides. Join EG, FH, EF, FG, GH and HE. Draw four arcs with radius $a/2$ and with centres A, B, C and D. Now the circle square composite system is divided into 32 segments and number them 1 to 32. 1 to 16 are of one dimension called S_1 segments and 17 to 32 are of different dimension called S_2 segments.



III. Calculations:

ABCD = Square; Side = a, EFGH = Circle, diameter = a, radius = $a/2$

$$\text{Area of the } S_1 \text{ segment} = \left(\frac{6 - \sqrt{2}}{128} \right) a^2 ; \text{ Area of the } S_2 \text{ segment} = \left(\frac{2 + \sqrt{2}}{128} \right) a^2 ;$$

$$\text{Area of the square} = 16 S_1 + 16 S_2 = 16 \left(\frac{6 - \sqrt{2}}{128} \right) a^2 + 16 \left(\frac{2 + \sqrt{2}}{128} \right) a^2 = a^2$$

$$\text{Area of the inscribed circle} = 16 S_1 + 8 S_2 = 16 \left(\frac{6 - \sqrt{2}}{128} \right) a^2 + 8 \left(\frac{2 + \sqrt{2}}{128} \right) a^2 = \left(\frac{14 - \sqrt{2}}{16} \right) a^2$$

$$\text{General formula for the area of the circle } \frac{\pi d^2}{4} = \frac{\pi a^2}{4} = \left(\frac{14 - \sqrt{2}}{16} \right) a^2 ; \text{ where } a = d = \text{side} = \text{diameter}$$

$$\therefore \pi = \frac{14 - \sqrt{2}}{4}$$

IV. How two formulae for S_1 and S_2 segments are derived ?

$$16 S_1 + 16 S_2 = a^2 = \text{area of the Square} \quad \dots \text{Eq. (1)}$$

$$16 S_1 + 8 S_2 = \frac{\pi a^2}{4} = \text{area of the Circle} \quad \dots \text{Eq. (2)}$$

$$(1) - (2) \Rightarrow 8S_2 = a^2 - \frac{\pi a^2}{4} = \frac{4a^2 - \pi a^2}{4} = S_2 = \frac{(4 - \pi)a^2}{32} = \frac{a^2}{32}(4 - \pi)$$

$$(2) \times 2 \Rightarrow 32 S_1 + 16 S_2 = \frac{2\pi a^2}{4} \quad \dots \text{Eq. (3)}$$

$$16 S_1 + 16 S_2 = a^2 \quad \dots \text{Eq. (1)}$$

$$(3) - (1) \quad 16S_1 = \frac{\pi a^2}{2} - a^2 = S_1 = \frac{a^2(\pi - 2)}{32} = \frac{a^2}{32}(\pi - 2)$$

V. Both the π values appear correct when involved in the two formulae

a) Official π value = 3.1415926...

b) Proposed π value = 3.1464466... = $\frac{14 - \sqrt{2}}{4}$

Hence, another approach is followed here to decide **real** π value.

VI. Involvement of line-segments are chosen to decide real π value.

A line-segment equal to the value of $(\pi - 2)$ in S_1 segment's formula and second line-segment equal to the value of $(4 - \pi)$ in S_2 segment's formula are **searched** in the above construction.

a) Official π : $\pi - 2 = 3.1415926... - 2 = 1.1415926....$

$$\text{Proposed } \pi : \pi - 2 = \frac{14 - \sqrt{2}}{4} - 2 = \frac{6 - \sqrt{2}}{4}$$

The following calculation gives a line-segment for $\frac{6 - \sqrt{2}}{4}$ and no line-segment for 1.1415926..

IM and LR two parallel lines to DC and CB; $OK = OJ = \text{Radius} = \frac{a}{2}$; JOK = triangle

$$JK = \text{Hypotenuse} = \frac{\sqrt{2}a}{2}$$

Third square = LKMC; $KM = CM = \text{Side} = ?$

$$KM = \frac{IM - JK}{2} = \left(a - \frac{\sqrt{2}a}{2} \right) \frac{1}{2} = \left(\frac{2 - \sqrt{2}}{4} \right) a; \quad \text{Side of first square DC} = a$$

$$DC + CM = a + \left(\frac{2 - \sqrt{2}}{4} \right) a = \left(\frac{6 - \sqrt{2}}{4} \right) a$$

b) Official $\pi = 4 - \pi = 4 - 3.1415926... = 0.8584074....$

$$\text{Proposed } \pi = 4 - \pi = 4 - \frac{14 - \sqrt{2}}{4} = \frac{2 + \sqrt{2}}{4}$$

No line-segment for 0.8584074... in this diagram.

MB line-segment is equal to $\frac{2 + \sqrt{2}}{4}$. How ?

Side of the first square CB = a

$$MB = CB - CM = a - \left(\frac{2 - \sqrt{2}}{4} \right) a = \left(\frac{2 + \sqrt{2}}{4} \right) a$$

VII. Conclusion:

This diagram not only gives two formulae for the areas of S_1 & S_2 segments and also shows two line-segments for $(\pi - 2)$ and $(4 - \pi)$. Line-segment is the soul of Geometry.